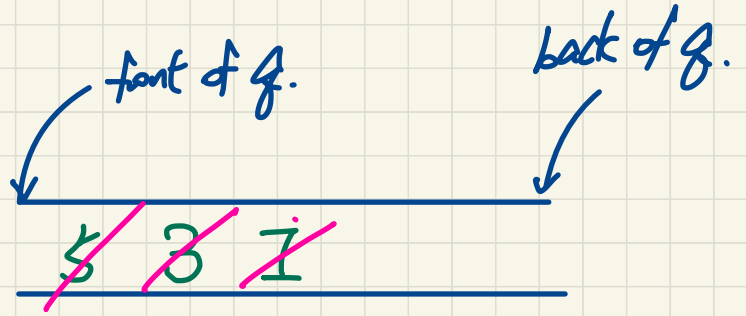


Queue ADT: Illustration

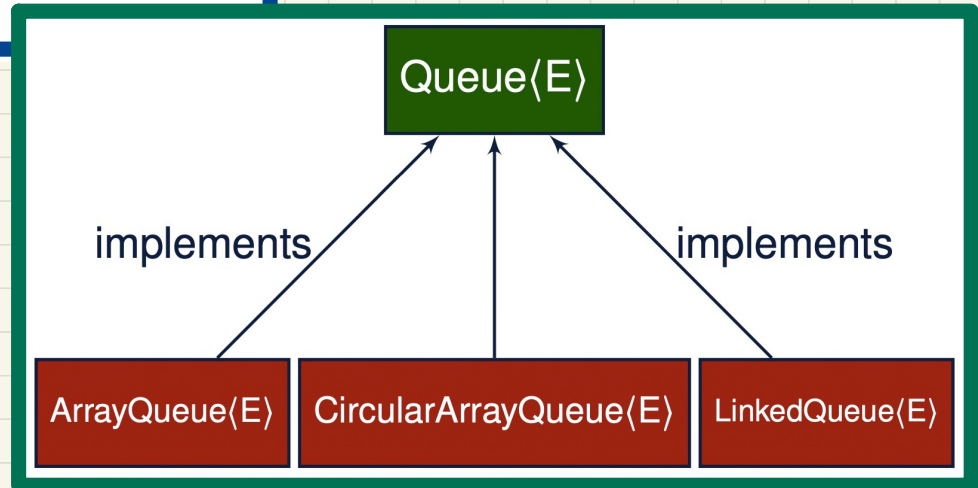
	isEmpty	size	first
<u>new queue</u>	T	0	n.a.
enqueue(<u>5</u>)	F	1	5
enqueue(<u>3</u>)	F	2	5
enqueue(<u>1</u>)	F	3	5
<u>rm. 5</u> dequeue	F	2	3
<u>rm. 3</u> dequeue	F	1	1
<u>rm. 1</u> dequeue	T	0	n.a.



First-In First-Out (FIFO)

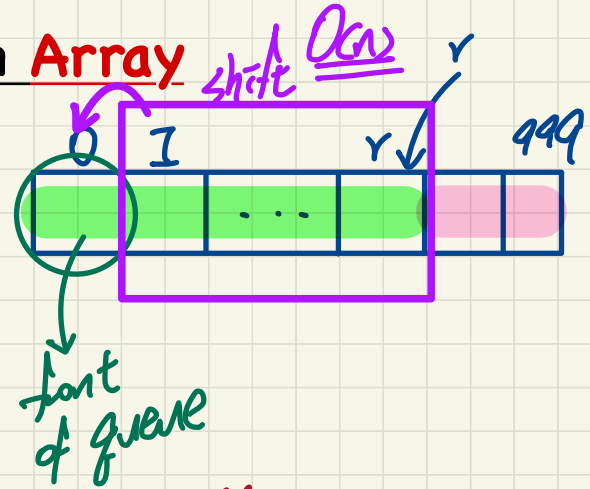
Implementing the Queue ADT in Java: Architecture

```
public interface Queue< E > {  
    public int size();  
    public boolean isEmpty();  
    public E first();  
    public void enqueue( E e);  
    public E dequeue();  
}
```



Implementing the Queue ADT using an Array

```
public class ArrayQueue<E> implements Queue<E> {
    private final int MAX_CAPACITY = 1000;
    private E[] data;
    private int r; /* rear index */
    public ArrayQueue() {
        - data = (E[]) new Object[MAX_CAPACITY];
        - r = -1;
    }
    • public int size() { return (r + 1); }  $O(1)$ 
    • public boolean isEmpty() { return (r == -1); }  $O(1)$ 
    • public E first() {
        if (isEmpty()) { /* Precondition Violated */ }
        else { return data[0]; }  $O(1)$ 
    }
    public void enqueue(E e) {
        if (size() == MAX_CAPACITY) { /* Precondition Violated */ }
        else { r++; data[r] = e; }  $O(1)$ 
    }
    public E dequeue() {
        • if (isEmpty()) { /* Precondition Violated */ }
        else {
            E result = data[0];
            for (int i = 0; i < r; i++) { data[i] = data[i + 1]; }  $O(n)$ 
            data[r] = null; r--;
            return result;
        }
    }
}
```



Limitation:
no resizing.

to improve this,
we need to be flexible
about where the front index
is $\Rightarrow$ Circular array.

shifting "2nd item"
and onwards
to the left by
one position

Implementing the Queue ADT using a SLL

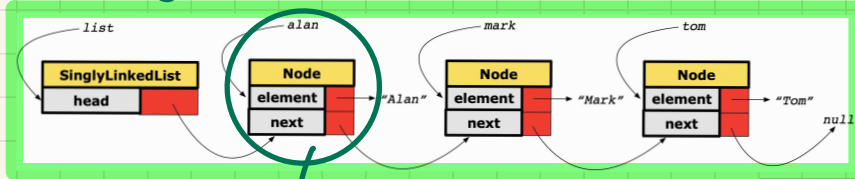
```
public class LinkedListQueue<E> implements Queue<E> {  
    private SinglyLinkedList<E> list;  
    ...  
}
```

$O(n)$

① use SL instead
② use DLL instead

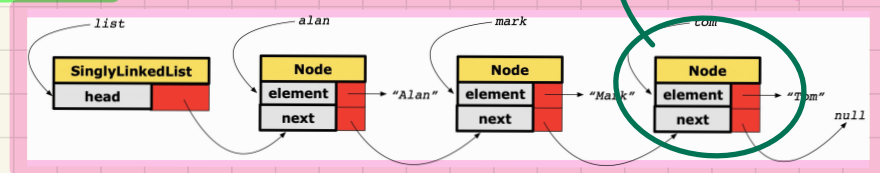
Queue Method	Singly-Linked List Method	
	Strategy 1	Strategy 2
size	list.size	list.size
isEmpty	list.isEmpty	list.isEmpty
first	list.first	list.last
enqueue	list.addLast	list.addFirst
dequeue	list.removeFirst	list.removeLast

Strategy 1

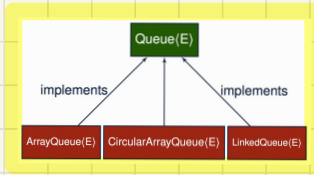


first of queue

Strategy 2



Stack ADT: Testing Alternative Implementations



```
public class ArrayQueue<E> implements Queue<E> {
    private final int MAX_CAPACITY = 1000;
    private E[] data;
    private int r = -1; /* rear index */
    public ArrayQueue() {
        data = (E[]) new Object[MAX_CAPACITY];
        r = -1;
    }
    public int size() { return (r + 1); }
    public boolean isEmpty() { return (r == -1); }
    public E first() {
        if (isEmpty()) { /* Precondition Violated */ }
        else { return data[0]; }
    }
    public void enqueue(E e) {
        if (size() == MAX_CAPACITY) { /* Precondition Violated */ }
        else { r++; data[r] = e; }
    }
    public E dequeue() {
        if (isEmpty()) { /* Precondition Violated */ }
        else {
            E result = data[0];
            for (int i = 0; i < r; i++) { data[i] = data[i + 1]; }
            data[r] = null; r--;
            return result;
        }
    }
}
```

dynamic binding.

```
@Test
public void testPolymorphicQueues() {
    Queue<String> q = new ArrayQueue<>();
    q.enqueue("Alan"); /* dynamic binding */
    q.enqueue("Mark"); /* dynamic binding */
    q.enqueue("Tom"); /* dynamic binding */
    assertTrue(q.size() == 3 && !q.isEmpty());
    assertEquals("Alan", q.first());

    q = new LinkedQueue<>();
    q.enqueue("Alan"); /* dynamic binding */
    q.enqueue("Mark"); /* dynamic binding */
    q.enqueue("Tom"); /* dynamic binding */
    assertTrue(q.size() == 3 && !q.isEmpty());
    assertEquals("Alan", q.first());
}
```

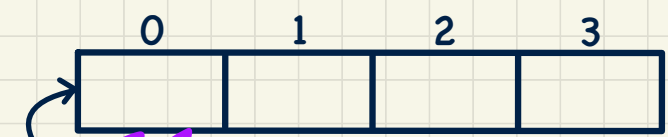
polymorphism

Size of queue vs. size of array % modulo

Implementing the Queue ADT using a Circular Array

Assume: A circular array of length 4.

Phase 0: Empty Queue q



$f=0$;
 $r=0$;

Empty Queue?

$r == f$

Phase 1: enqueue 3 elements

$data[r] = item$;
 $r++$;



$[f, r-1] =$
 $(r-1) - f + 1 =$
 $r - f$



empty slots before this index
slots before this index

Size: $r > f$

$r - f$

Queue Full? $(r+1) \% N$
when r points to 3 is the only empty slot.

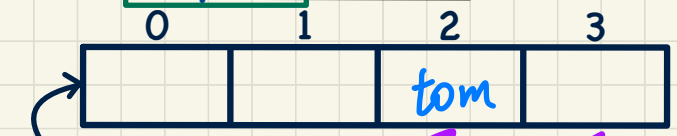
1. fix-sized (no resizing)

Circular Array

2. flexible for performing "dequeue"

$data[f] = null$; $f++$;

Phase 2: dequeue 2 times

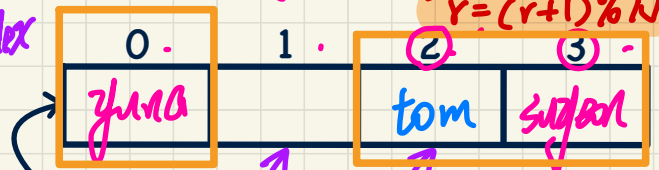


Size: $3 - 2 = 1$

Size of array: 4 (fixed)
Size of q: 1

Phase 3: enqueue 2 elements

$data[r] = item$;
 $r++$;
 $r = (r+1) \% N$



Size: $r < f$
 $r + (N - f)$

$[0, r-1]$
 $(r-1) - 0 + 1 =$
 r

$[f, N-1]$
 $(N-1) - f + 1 =$
 $N - f$